# LIGHTLY REINFORCED WALLS SUBJECTED TO MULTI-DIRECTIONAL SEISMIC EXCITATIONS: INTERPRETATION OF CAMUS 2000-1 DYNAMIC TESTS

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#### ABSTRACT

In this paper, the study of the inelastic seismic performance of a 5-storey reinforced concrete wall specimen, which was tested under bi-directional seismic excitations is presented. The structure has been sized and detailed following the French PS92 code, where the reinforcement is just designed so as to have the same strains at several levels. To investigate the simplifying assumptions made in design, and to assess the validity of the numerical tool, a 3-D refined non-linear analysis was conducted. Due to the out-of-plane excitation, high variation of axial force results in smaller bending capacity. Since good correlation is obtained between calculated and test results, the numerical model is then used to predict the seismic response when only one-directional excitation is applied, or when vertical component is added to the other two horizontal components. In the presence of vertical excitation, additional variation of the axial force is to be expected.

**KEYWORDS:** Lightly RC Wall, Bi-directional Seismic Loading, 3-D Finite Element Analysis, Shaking-Table Test

## **INTRODUCTION**

In the past two decades, extensive experimental and analytical research on the seismic behaviour of RC wall structures has been conducted mainly in USA, Japan, New Zealand and Europe (ASCE, 1982; Vulcano et al., 1988). Nearly all these experimental and analytical studies have concentrated on the seismic behaviour of walls designed and detailed to develop a ductile flexural plastic hinge only at the base. Very little attention has been paid to the seismic behaviour of lightly reinforced RC walls.

RC bearing walls with limited reinforcement ratio are commonly used in France and some central European countries for the building structures. In wall structures, as masonry is generally not used for partitioning, walls arrangement is redundant when compared to the structural demand. In this kind of structures, an alternative design procedure may be adopted: instead of "localizing" damage at the base, the wall can be allowed to go inelastic and develop cracking and/or plastic hinges at any location along its height. Slender walls may be designed in this way as lightly reinforced walls, the flexural reinforcement being curtailed in accordance with the bending moment diagram. Besides the lower costs corresponding to the limited reinforcement ratio, this technique seems to be able to ensure an adequate seismic behaviour.

Within the French CAMUS (Bisch and Coin, 1998) and European TMR (Training and Mobility of Researchers) projects (www.cordis.lu/tmr/home.html), shaking table tests on RC wall structures in different situations (fixed or not to the shaking table, placed on a layer of sand, with different reinforcement ratio, etc.) have been performed. The data provided by these experimental programs have been used not only to validate numerical models integrated on FE codes (Mazars, 1998; Faria et al., 2002; Fischinger et al., 2002) but also to improve existing design methods (Bisch and Coin, 1998). During the current conversion of Eurocode 8 into a standard (EN1998-1: Design of Structures for Earthquake Resistance), "large lightly reinforced walls" have been introduced along with the ductile walls present in the ENV (prestandard) version of EC 8 (Fardis, 2000).

It is to be noted that, in these research programs, only loadings in one direction (in the plane of the walls) were applied. In real structures, such walls are likely to be loaded in the out-of-plane direction as well and then, the question arises, how such walls behave under combined in-plane and out-of-plane

loading. Moreover, no exhaustive studies have been conducted so far for this combination of loadings that can be extremely severe for wall structures.

A new research program CAMUS 2000 was launched in 1998 with the aim of evaluating the effects of torsion and the behaviour of lightly reinforced walls subjected to bi-directional motions. As a part of the program, two scaled (1/3) models representative of 5 storeys reinforced concrete buildings have been tested on the major Azalee shaking table of Commissariat à l'Energie Atomique CEA (France) in the Saclay Nuclear Centre. The first structure (CAMUS 2000-1) has been subjected to horizontal bi-directional excitations. Two identical shear walls in one direction and a steel bracing system in the orthogonal direction provided structural stiffness. For the second test (CAMUS 2000-2), an in-plane excitation was applied (Combescure et al., 2002). A torsional response was caused by the fact that the two walls have different lengths.

The objective of this work is to verify the design assumptions and to obtain more detailed information about the behaviour of walls with limited reinforcement when subjected to bi-directional earthquake motions. The first step consists of the 3-D numerical analysis of the seismic response of the CAMUS 2000-1 specimen. By comparing experimental and non-linear analysis results, the accuracy and efficiency of the computational tool is verified under bi-directional horizontal seismic loading. In further analyses, the numerical model is used to predict the seismic response when only one in-plane horizontal excitation is applied, or when vertical component is added to the other two horizontal components.



Fig. 1 General scheme of the CAMUS 2000-1 specimen (dimensions in meters)

#### **DESIGN OF THE TEST SPECIMEN**

One of the objectives of the CAMUS 2000 research has been that of examination of the influence of bi-directional seismic excitations on the inelastic behaviour of in-plane regular wall structures. Due to the acceleration perpendicular to the wall plane, simultaneous to the in-plane acceleration, more damage is to be expected at cracks closure. Owing to very low reinforcement ratio and to the reinforcement yielding, steel-reinforcing bars may rapidly lose the capability of maintaining adjacent wall elements (i.e. separated by a crack) in a plane movement at load reversal. To study these effects, the test specimen has been designed as lightly reinforced and has been subjected to two horizontal uncorrelated accelerograms in the *X* and *Y* directions (Figure 2). Since the research is more oriented towards the knowledge of the behaviour of lightly reinforced walls, there was no need to deduce the dimensions of the specimens directly from a reference building. However, it was considered as necessary that the general characteristics of the

specimen can be deduced from elements, which can be found in a real building, in order to ensure a reasonable representativeness. So, five storeys have been considered as representative of the current situation in France, and a scale factor of 1/3 has been chosen.

For the definition of the maximum seismic action, due consideration has been given to the specimen's strength in the perpendicular direction of the walls. As a matter of fact, this strength is that of the composite steel – concrete bracing system in the *Y* direction, which has been defined at the beginning of the previous CAMUS research programs (Bisch and Coin, 1998). With a PS92 (REGLE, 1995), specified seismic action defined by the NICE S1 PS92 design spectrum, the specimen has been designed for a peak ground acceleration (PGA) of about 0.51*g* and to a behaviour factor q = 3.73 (Bisch and Coin, 2002). The flexural reinforcement has been determined considering the existence of possible higher values for the tensile and compressive axial force in each wall, due to the out-of-plane loading effect. To enforce a predominantly flexural behaviour with nearly horizontal cracking all along the height of the walls, the flexural reinforcement has been optimised in each quarter of each level. Figure 1 indicates the flexural reinforcement distribution as well as the reinforcement ratio at the base of each storey. Verification under shear force indicated that the amplified designed shear is less than the design shear strength without reinforcement, so the specimen has no horizontal shear reinforcement.

The specimen is composed of two parallel 5-floor RC walls without openings, linked together by 6 square floors, the reinforced concrete footing being anchored to the shaking table (Figure 1). The walls are each 5.10 m high, 1.70 m long and 6 cm thick. They were cast in order to reproduce the construction joints at the level of each floor. All the floors are 1.70 m long, 1.70 m wide, and 21 cm thick. The wall footing is 2.10 m long, 0.60 m high and 10 cm thick. Additional mass was added to the upper and lower parts of each floor (excepting the first floor) as well as on the walls at mid-height of each level, to simulate the gravity load compatible with the vertical stress values commonly found at the base of this type of structure (about 1.6 MPa). The steel bracing system stabilising the structure in the direction perpendicular to the walls is shown in Figure 2. It is designed in such a way that the two walls carry the entire vertical load. Only four steel bars acting in traction and compression connect the lateral bracing system of two different storeys.



Fig. 2 Steel bracing system for CAMUS 2000-1 specimen (dimensions in centimeters)

## SEISMIC ACTION

The specimen was tested on the AZALEE shaking table, in the CEA facilities, which allows for testing 100 t models under three directional excitations. During the shaking table tests, the specimen was subjected to increasing horizontal artificial accelerations along the direction parallel and perpendicular to the walls plane. The following PGA levels of the uncorrelated input signals were applied during the test in

both directions: 0.15g, 0.40g, 0.55g and 0.65g. The input signals have been derived from the French PS92 spectrum S1, with a PGA of 2.5 m/s<sup>2</sup>. Figure 3 shows the reference acceleration signals and the corresponding acceleration response spectra for 5% damping.



Fig. 3 Reference signals and acceleration spectra (5% damping)

# **BEHAVIOUR OF THE SPECIMEN**

## 1. Axial Force

Previous experimental and numerical studies on lightly reinforced walls subjected to in-plane uni-directional loading (Bisch and Coin, 1998; Ile et al., 2002) have underlined the importance of the variation of the dynamic axial force. The first cause of this phenomenon is the extension mode due to bending: at maximum horizontal deflection, the neutral axis is at its maximum distance from the centre of the wall cross-section, the raising of masses is maximum and the dynamic variation of the axial force is a tensile force; the frequency of this vertical motion is twice that of the horizontal movement. The second reason of this phenomenon relies on the excitation of the first natural vertical mode of the system: at cracks closure, when concrete recovers its stiffness, compression forces strongly increase and these shocks excite the vertical vibration mode of the system (shaking table + specimen). It is to be noted that the variation of the axial force affects the value of the maximum bending moment, as these two parameters act together to determine the ultimate state of strain in the wall. Therefore, axial force variation has to be taken into account in design. In conclusion of the previous CAMUS research (Fouré and Vié, 2002a, 2002b), the following principle has been proposed in order to introduce the axial force in design:

• In the first phase, the design is made with the static value of the axial force,  $N_0$ , and the corresponding value of the ultimate bending moment,  $M_{ult}$ . The extreme strains at the section level

are  $\varepsilon_a$  and  $\varepsilon_b$ , where  $\varepsilon_a$  stands for the tensile steel strain and  $\varepsilon_b$  for the compressive concrete strain. At least one of these two strains represents an ultimate strain corresponding to a limit state of the reinforced concrete section. For lightly reinforced walls, with low axial compression, this limit state generally corresponds to the code specified value  $\varepsilon_{au} = 10 \times 10^{-3}$ .

In the second phase, the variation ±ΔN of the axial force is considered. With the assumption that the curvature is constant, a new limit state is found, corresponding to M'<sub>ult</sub> = M<sub>ult</sub> + ΔM and to the extreme strains ε<sub>a</sub> + Δε<sub>G</sub> and ε<sub>b</sub> + Δε<sub>G</sub> (Δε<sub>G</sub> being the neutral axis translation due to the variation of the axial force). If the compressive strain in concrete is excessive (> 3.5×10<sup>-3</sup>), either the width of the wall is increased, or the concrete is confined. If the tensile strain in the steel bars is excessive, the reinforcement area has to be increased.

The range of variation of the axial force is difficult to be known a priori because it depends on the vertical response of the structure and mainly on the vertical accelerations. However, until further information from extensive parametric studies is available, the following formula for estimating the axial force variation has been proposed and accepted in the prestandard version of EC 8 (pr EN 1998-1, final project team, December 2001):

$$\Delta N_{\rm max} = \pm \lambda N_0$$

where  $\lambda$  depends on the soil type, and on the ratio  $T_A/0.5T_F$ ,  $T_A$  being the horizontal vibration period and  $T_F$  the vertical vibration period of the structure.

Since the CAMUS 2000-1 specimen is subjected to bi-directional loading, the overturning moment perpendicular to the walls induces a complementary axial force in one wall and a tensile axial force in the other. The total axial force variation in each wall is then given by the superposition of the dynamic axial force due to the in-plane bending and of the axial force due to the out-of-plane loading. Based on previous experimental results on lightly reinforced walls, and taking into account the uncertainty of the dynamic axial force variation, design has assumed  $\lambda = 0.8$ . According to the two design combinations rules,  $S_x + 0.3S_y$  and  $S_y + 0.3S_x$  (where  $S_x$  and  $S_y$  are action effects), the maximum axial force  $(N_r)$  due to the out-of-plane loading in each wall has been calculated. Its design value is equal to ±192 kN. The total variation of the axial force in each wall is then given by:

$$\Delta N_{\rm max} = \pm \lambda N_0 \pm N_r = \pm 343 \,\rm kN, (N_0 = 180.7 \,\rm kN)$$

This large variation (almost double of the permanent load) indicates that different states of cracking from one wall to another are to be expected, leading to different lengthening of their neutral axis and asymmetric behaviour of the specimen.

## 2. Torsional Stiffness of the Floors

Due to the out-of-plane loading, the torsional mode also is expected to be excited as soon as inelastic behaviour is observed. At each level of the construction, the rotations of the wall sections are not the same and rotation of the floors about a vertical axis is involved in the behaviour. At each level, the floors are then able to transfer a bending moment from one wall to the other. It is to be noted, however, that in the case of CAMUS 2000-1 specimen, the thickness of the floors (21 cm) was determined in order to provide the necessary floor strength under the weight of additional masses. This value is much higher than that in a real construction. Since the usual thickness of floors is about 18 cm in a normal building, taking into account a scale factor of 3, the thickness of the specimens' floors should have been 6 cm. Hence, the stiffness of the floors is much higher in the specimen than in a normal building and the twist rotation is expected to be much lower than in a real situation. Considering also the fact that the two perpendicular excitations are uncorrelated and maximum action effects do not generally occur at the same instant of time, the horizontal top displacements of the two walls should be different, because the out-of-plane loading creates unequal axial forces in the two walls.

It is clear that axial force effects as well as re-distribution of forces due to the evolution of stiffness of the walls are completely non-linear and cannot be adequately represented in a standard linear elastic model. One aim of the non-linear time history analysis is to verify these design assumptions and to obtain more detailed information about the behaviour of the specimen.

## **MODELLING APPROACH**

The numerical analyses have been performed using the general-purpose finite element program CASTEM 2000 developed at CEA-Saclay, France. To predict the inelastic seismic response with sufficient accuracy, due care has been given to create detailed model of the specimen, taking into account the necessary geometric characteristics, construction details and boundary conditions. An example of the 3-D finite element mesh used in the analyses is reported in Figure 4. Due to the direction of the applied loading, in-plane as well as out-of-plane behaviour of the walls need to be analysed. Therefore, layered thin shell discrete Kirchoff triangles (DKT) are used to represent the two walls and the slabs. The shaking table is modelled with solid eight-node brick elements, while four-node shell elements are used to model the steel I-shaped bracing system. A discrete modelling is adopted to represent the reinforcement through the use of two-node truss-bar elements. The structure is assumed fully restrained at all nodes along the base of the shear wall. During previous tests on CAMUS specimens (Sollogoub et al., 2000), it was observed that the specimen oscillations have induced vertical and rocking displacements on the shaking table, leading to significant reductions of the corresponding natural frequencies. In these conditions, the shaking table itself in terms of mass and their external supports in terms of stiffness had to be included into the numerical model. Owing to its high stiffness, the finite elements representing the shaking-table were assumed to remain elastic and almost infinitely rigid. The total mass, 25000 kg, of the shaking-table was uniformly distributed to these finite elements. The vertical rods, supporting the shaking-table, were simulated by four elastic vertical bars, the axial stiffness of each bar being equal to 215 MN/m, as suggested by experimenters. Perfect bond was assumed to exist between concrete and reinforcement. The possibility of non-linear material behaviour was specified for all wall concrete and reinforcing barelements, while the behaviour of the foundation and bracing system was considered as elastic. Assuming a 2.5% critical damping factor (close to the measured damping value) for the first and second vibration modes, the damping parameters,  $\alpha$  and  $\beta$ , were calculated and used subsequently to form the Rayleigh damping matrix  $[C] = \alpha [M] + \beta [K]$ , M and K being the mass and stiffness matrices. Despite the fact that a modal characterisation is theoretically correct only for linear elastic systems, the damping matrix [C] obtained in this way is assumed to remain constant throughout the loading cycle. To solve the non-linear equilibrium equations, a modified Newton-Raphson iteration solution scheme was used.



Fig. 4 3-D finite element mesh of the CAMUS 2000-1 specimen

#### **CONSTITUTIVE MODELS AND MATERIAL PARAMETERS**

In order to achieve a good compromise between simplicity and accuracy, a biaxial concrete model that provides acceptable representation of the cyclic inelastic behaviour of reinforced concrete under cyclic loading was used. This model (Merabet and Reynouard, 1999) adopts the concept of a smeared crack approach with a possible double cracking only at 90°. It is based upon the plasticity theory for uncracked concrete with isotropic hardening and associated flow rule. Two distinct criteria describe the failure surface: Nadai in compression and bi-compression and Rankine in tension. Hardening is isotropic and an associated flow rule is used. When the ultimate surface is reached in tension, a crack is created perpendicularly to the principal direction of maximum tensile stress, and its orientation is considered as fixed subsequently. Each direction is then processed independently by a cyclic uniaxial law, and the stress tensor in the local co-ordinate system defined by the direction of the cracks is completed by the shear stress, elastically calculated with a reduced shear modulus  $\mu G$  (with  $0 < \mu < 1$ , and  $\mu$  being a function of the crack opening strain), to account for the effect of interface shear transfer:

$\mu = 0.4$	if $\varepsilon_{cr} - \varepsilon_{res} - \varepsilon_{tm} \leq 2\varepsilon_{tm}$
$\mu = 0$	if $\varepsilon_{cr} - \varepsilon_{res} - \varepsilon_{tm} \ge 2\varepsilon_{tm}$
$\mu = 0$ and $\sigma_{12} = 0$	if $\mathcal{E}_{cr} - \mathcal{E}_{res} - \mathcal{E}_{tm} \geq 4\mathcal{E}_{tm}$

where

 $\mathcal{E}_{cr}$  - total strain,

 $\mathcal{E}_{res}$  - residual strain after unloading in compression,

 $\mathcal{E}_{tm}$  - crack opening strain, and

 $\sigma_{tm}$  - shear stress.

The behaviour of a point initially under tension, which completely cracks prior to undergoing a reverse loading in compression, is illustrated in Figure 5. Similar laws describe the case of an initial compressed point or that of a point, which has not totally cracked under a reverse loading. The model has been described in detail and verified elsewhere. Its validity has been demonstrated by using it to predict the behaviour of shear walls with different span-to-height ratio under monotonic, cyclic and dynamic loading conditions for which experimental observations were available (Ile and Reynouard, 2000; Ile et al., 2002).



Fig. 5 Uniaxial model: Point initially in tension

For steel, a cyclic model that can take into account the Bauschinger effect and buckling of reinforcing bars has been adopted (Figure 6). The monotonic branch is characterised by an initial linear branch

followed by a plateau and hardening up to failure. The cyclic behaviour is described by the formulation proposed by Giuffré and Pinto and implemented by Menegoto and Pinto (1973). A detailed description of the steel constitutive law can be found in Guedes et al. (1994).









Fig. 6 Numerical model for steel under cyclic loading

The evaluation of steel parameters was quite simple, the measured elasticity modulus - 200000 MPa, yield stress - 664 MPa, failure stress - 733 MPa, and strain at failure - 2.2%, being directly used. For concrete, the material properties were generally as provided by the CAMUS 2000-1 experimental data (Fouré and Vié, 2002a, 2002b) and design codes:  $E_c = 23000$  MPa for the initial elastic modulus, 34 MPa for the compressive strength, and 2.6 MPa for the tensile strength. An initial value of 0.40 for the post-cracking parameter,  $\mu$ , was assumed in the analysis. In order to calibrate the first two experimentally observed natural frequencies (5.8 Hz in the out-of-plane direction and 6.25 Hz in the direction parallel to the walls), it was necessary to adopt a reduced elastic modulus for the footing  $(E_c/3.0)$ .



Fig. 7 Comparison between calculated and measured horizontal relative top displacements for PGA = 0.15g: A) Average in-plane relative displacement; B) Out-of-plane relative displacement



Fig. 8 Comparison between calculated and measured horizontal relative top displacements for PGA = 0.40g: A) Average in-plane displacement; B) Out-of-plane displacement

#### **BI-DIRECTIONAL (XY) EXCITATION: COMPARISON WITH EXPERIMENTAL RESULTS**

The comparison of the numerical time history results with the experimental records is one important step in confirming the accuracy of the modelling approach. Numerical results also allow to verify design assumptions and to extend the limited experimental database of seismic wall behaviour with analytical data. The experimental bending moments, shear forces and axial forces have been computed with the absolute accelerations given by the accelerometers and the estimation of the masses of each floor. Due to the fact that the structure is hyperstatic the experimental internal forces in each wall were difficult to be estimated. Based on the assumption that the RC floors can transfer only torsion and no bending (due to the high out-of-plane flexibility in bending of the walls), the measurement channels used during the test allowed determining with sufficient accuracy only horizontal (shear) and normal (axial) forces in each wall (Combescure, 2002). The experiment could also indicate the total bending moment at different levels for the whole specimen, but the values of the bending moment in each wall, which are however important, were not measured. Since the numerical model can indicate individual bending moments at specified locations in each wall, its usefulness in investigating the wall behaviour is obvious.

In the numerical analysis, all the seismic signals applied to the specimen were considered in chronological order. Both numerical and experimental results showed that the relative top in-plane horizontal displacements of the two walls were similar, due to the high stiffness of the floors. Therefore, comparison of relative displacements in X direction concerns only average time history values of the two walls. First comparisons presented in Figures 7 to 10 concern relative horizontal displacements in X (inplane) and Y (out-of-plane) directions. As can be seen, the correlation between analysis and experiment is generally very satisfactory, even for very high transient input motions. It should be noted, however, that for PGA = 0.65g the amplitude of the relative out-of-plane displacement is underestimated and the response frequency is overestimated by the numerical model. Actually, during this last test, failure of the connection of the bracing system with the slab was observed, one branch of the bracing system being completely dislocated from the slab. This was probably due to a higher out-of-plane shear force than that anticipated in design. Since the behaviour of this connection was considered as elastic in the analysis, the observed discrepancies between experimental results and analysis seem normal. The analysis predicted failure of the specimen by rupture of one reinforcing bar for a relative horizontal in-plane displacement of about 2.5 cm, the maximum recorded relative displacement being around 5.0 cm. A complete analytical time-history response is not provided in Figure 10, because analysis was stopped after the rupture of the steel bar due to the difficulties in obtaining the convergence at this stage. Further comparisons are also

shown in Figures 11 and 12 for the same specimen subjected to PGA = 0.55g input signal. Again, the analytical axial force in each wall and the total bending moment at the base of the first level agree reasonably well with the experimental results.

Local results as obtained from the dynamic analysis are shown in Figure 13. This figure depicts the damage distribution obtained just after one of the steel bars of the left wall has broken in tension. The analysis results indicate that damage is almost entirely concentrated just under the  $2^{nd}$  floor level, and highlight the fact that crack opening is larger for the wall which is in tension as compared to the wall which is in compression. This seems to be in reasonable agreement with what was experimentally observed: at failure, a wide crack opens under the  $2^{nd}$  floor level and inspections after the test show that the steel bars are broken at this level (see Figure 13).



Fig. 9 Comparison between calculated and measured horizontal relative top displacements for PGA = 0.55g: A) Average in-plane displacement; B) Out-of-plane displacement



Fig. 10 Comparison between calculated and measured horizontal relative top displacements for PGA = 0.65g: A) Average in-plane displacement; B) Out-of-plane displacement



Fig. 11 Comparison between calculated and measured axial force at the base of the first storey for one wall (PGA = 0.55g): A) Left wall; B) Right wall



Fig. 12 Comparison between calculated and measured bending moment at the base of the first storey for two walls (PGA = 0.55g)

Figures 14 to 21 present numerical results in terms of bending moment-axial force interaction diagrams at two critical sections, together with the variation of axial load and moment. Figure 22 shows the experimental first storey bending moment-relative displacement relationship for the last two input motions. It can be observed that the limit state in each of the two walls seems to be attained for the last two accelerations levels of 0.55g and 0.65g. The differences between these two last tests concern only the displacements and strains and the behaviour of the specimen is very similar to that of a ductile structure, the value of the PGA to be resisted by the structure being a function of the maximum strain attained in the constitutive materials. It is also to be noted that two plastic hinges tend to form at two critical sections (bases of the 1<sup>st</sup> and 2<sup>nd</sup> storeys) and that this aspect confirms the design intention, which aimed at distributing the damage over the height of the structure. However, the fact that the analysis predicted failure only at one critical section (the base of the 2<sup>nd</sup> storey) indicates that it is almost impossible to attain simultaneously the ultimate strains in all potential plastic hinges.



Vertical concrete strain contours at failure

Crack pattern at the end of the test



Table 1 shows a comparison between the design and numerically predicted maximum response parameters with test results. It is to be noted that numerical analysis gives maximum response values, which are much closer to the test results, than the design values. This is due to the fact that the behaviour of the walls is highly non-linear and the equivalent linear analysis is not able to represent the real dynamic behaviour of the specimen. Nevertheless, the design method was able to give good results in terms of ultimate PGA, because failure of the specimen was obtained for a higher PGA (0.65g) than that assumed in design (0.51g). It is also worth mentioning here that no lateral sliding has appeared during the shaking table tests and that the specimen was still able to sustain the vertical load at the end of the tests. The overly conservative design can be explained by the following facts:

- during seismic response, the stiffness of the floors may have a favourable effect on the ultimate strength of the structure, by redistributing forces between the two walls.
- the actual reinforcing steel yield strength (664 MPa) is higher than that assumed in design (500 MPa).
- design has assumed  $\lambda = 0.8$ . This leads to a much higher value of the axial force variation as compared to the test and numerical analysis results (Table 1).

All these aspects indicate that the design method is adequate, but the  $\lambda$  value assumed for the CAMUS 2000-1 specimen seems somehow too high. Based on numerical analysis results (also confirmed by test results), it is believed that if, for this particular case, a value of  $\lambda$  between 0.5-0.6 had been adopted, it would have led to a more realistic estimation of the ultimate design PGA. It is to be remarked that the 3-D non-linear analysis has predicted very consistent results in terms of axial force variation, hence design has to be based on non-linear analysis. However, since these results correspond to a specific case, systematic parametric studies considering a wider variety of geometric configurations and boundary conditions are still needed, in order to provide realistic bounds for the variation of the axial force to be taken into account in design.

	Design (0.51g)	Numerical Analysis (0.55g)	Test (0.55g)
In-plane relative top displacement (cm)	2.0	1.74	1.73
Out-of-plane relative top displacement (cm)	1.9	2.50	2.80
Bending moment at the bottom of the two walls (kN-m)	348	445	473
Variation of axial load at the bottom of the left wall (kN):			
+ Axial tensile force	+343	+299	+244
- Axial compression force	-343	-245	-273
Variation of axial load at the bottom of the right wall (kN):			
+ Axial tensile force	+343	+277	+251
<ul> <li>Axial compression force</li> </ul>	-343	-275	-294

Table 1: Maximum Response Values from Design, Analysis and Test



Fig. 14 Bending moment – axial force interaction diagrams and variation of bending moment and axial force at the base of the  $1^{st}$  storey (PGA = 0.15g)



Fig. 15 Bending moment – axial force interaction diagrams and variation of bending moment and axial force at the base of the  $2^{nd}$  storey (PGA = 0.15g)



Fig. 16 Bending moment – axial force interaction diagrams and variation of bending moment and axial force at the base of the  $1^{st}$  storey (PGA = 0.40g)



Fig. 17 Bending moment – axial force interaction diagrams and variation of bending moment and axial force at the base of the  $2^{nd}$  storey (PGA = 0.40g)



Fig. 18 Bending moment – axial force interaction diagrams and variation of bending moment and axial force at the base of the  $1^{st}$  storey (PGA = 0.55g)



Fig. 19 Bending moment – axial force interaction diagrams and variation of bending moment and axial force at the base of the 2nd storey (PGA = 0.55g)



Fig. 20 Bending moment – axial force interaction diagrams and variation of bending moment and axial force at the base of the 1st storey (PGA = 0.65g)



Fig. 21 Bending moment – axial force interaction diagrams and variation of bending moment and axial force at the base of the  $2^{nd}$  storey (PGA = 0.65g)



Fig. 22 First storey total bending moment – top relative displacement relationship

#### **COMPARISON OF RESPONSE DUE TO UNI- AND BI-DIRECTIONAL EXCITATION**

In addition to analyses with bi-directional excitations (XY-excitation), analyses with uni-directional acceleration (X-excitation) applied in the direction of the walls were also performed. Since there is not much difference (up to 5%) in the relative horizontal X displacement between the two cases, it can be concluded that the influence of the out-of-plane excitation on displacements is negligible. However, much more differences are observed when examining the bending moment and axial force at a critical section level. As can be seen in Figure 23, in case of X-excitation, the axial forces are close to  $N_0$ , because no out-of-plane loading was applied and axial force variation is only due to the dynamic axial force induced by the in-plane bending. In this case, failure does not occur, although the internal force couple is close to the limit. The situation is quite different in case of XY-excitation, due to the asymmetric behaviour of the specimen: while compression in one of the walls increases the stiffness of cracked sections, in the other wall compression decreases or even traction appears which makes the wall more flexible, increasing cracking of concrete and yielding of reinforcement. In the case of PGA = 0.65g, such unfavourable combination of forces caused rupture of reinforcement at one of the edges of the left wall, while rupture did not appear either in the right wall or in the uni-directional case. This case shows that during the seismic response, the increase in the strain demand when the compressive axial force is much lower than the permanent load  $(N_0)$  may be significant. The bending moment-curvature relationship for the critical section (under the 2nd storey) is shown in Figure 24. Before rupture, substantially lower yielding moment was obtained in the left wall (wall in tension) than in the right wall (wall in compression) or in the case of X-excitation. In the case of XY-excitation, the maximum moments in the right wall are somewhat higher than those in the case of X-excitation.

## COMPARISON OF RESPONSE DUE TO TRI- AND BI-DIRECTIONAL EXCITATION

In further analyses, vertical component of excitation was added to the two horizontal components (*XYZ*-excitation). The peak vertical ground acceleration amounted to 70% of the peak ground acceleration in the horizontal directions and the acceleration was so generated that its peaks were uncorrelated with those of the horizontal components. As in the previous case, maximum relative displacements obtained for *XYZ*- and *XY*-excitations do not show much difference (up to 4%). The damage pattern is almost the same and rupture occurs at the same reinforcement bar and practically at the same instant of time. There are, however, larger differences in the axial forces, because in the case of *XYZ*-excitation, the axial force at failure is close to 0, while in the bi-directional case, the axial force is a compressive force equal to

about 83 kN (Figure 23). Therefore, in the case of *XYZ*-excitation, somewhat lower ultimate moments and larger curvatures were obtained at failure than in the case of *XY*-excitation (Figure 24). In assessing the above results, it should be noted that this limited study is not intended to suggest any range of variation of the axial force to be considered in design, in recognition of the presence of vertical ground motion. The work is rather intended to highlight the significance of the vertical input for lightly reinforced walls, which has thus far been neglected. The fact that the increase in axial load variation may have a detrimental effect on the bending moment and possibly on the shear capacity suggests, at the very least, that further studies are required.



Fig. 23 Bending moment – axial force interaction diagrams and variation of axial force and bending moment at the base of the 2nd storey (PGA = 0.65g)



Fig. 24 Bending moment – curvature relationship at the base of the  $2^{nd}$  storey (PGA = 0.65g)

## **CLOSING REMARKS**

This paper describes the seismic behaviour of a lightly reinforced wall specimen under bi-directional loading. The significant effect of the wall degradation on the stiffness and strength of the wall suggests that it is always important that design procedures are derived from analytical modelling and experimental observations. This is due to the fact that axial force effects as well as re-distribution of forces due to the evolution of stiffness of the walls are completely non-linear and cannot be adequately represented in a standard linear elastic model. The experimental analytical comparisons not only demonstrate the accuracy of the time-history analysis model, but also allow obtaining more detailed information about the behaviour of the specimen when it is subjected to different loading conditions. By comparison with the uni-directional excitation, bi-directional excitation can importantly increase the strain demand of reinforced concrete walls with limited reinforcement, mainly because of increasing the variation of the axial force. In the case the excitation is introduced also in the vertical direction, additional variation of the axial force is to be expected. Since this study was concerned with a particular case, it is clear that more systematic and parametric studies, considering a wider variety of geometric configurations and boundary conditions, will be required to establish definite criteria for efficient designs of lightly reinforced walls. Based on the results obtained in this study, it appears possible to investigate behaviour trends for a wider variety of configurations than is practically possible to study experimentally.

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